

You downloaded this paper through cbse.biz

Blue Print III X - Mathematics

Unit / Form of Questions	VSA (1 Mark) each	SA - I (2 Marks) each	SA - II (3 Marks) each	LA (6 Marks) each	Total
Number systems	1(1)	--	3(1)	-	4(2)
Algebra	3(3)	2(1)	9(3)	6(1)	20(8)
Trigonometry	1(1)	2(1)	3(1)	6(1)	12(4)
Coordinate Geometry	-	2(1)	6(2)	-	8(3)
Geometry	2(2)	2(1)	6(2)	6(1)	16(6)
Mensuration	1(1)	-	3(1)	6(1)	10(3)
Statistics and Probability	2(2)	2(1)	-	6(1)	10(4)
Total	10(10)	10(5)	30(10)	30(5)	80(30)

Sample Question Paper III
Mathematics - Class X

Time : Three hours

Max. Marks : 80

General Instructions :

1. All Questions are compulsory.
 2. The question paper consists of thirty questions divided into 4 sections A, B, C and D. Section A comprises of ten questions of 01 mark each, section B comprises of five questions of 02 marks each, section C comprises of ten questions of 03 marks each and section D comprises of five questions of 06 marks each.
 3. All questions in Section A are to be answered in one word, one sentence or as per the exact requirement of the question.
 4. There is no overall choice. However, internal choice has been provided in one question of 02 marks each, three questions of 03 marks each and two questions of 06 marks each. You have to attempt only one of the alternatives in all such questions.
 5. In question on construction, drawings should be neat and exactly as per the given measurements.
 6. Use of calculators is not permitted. However, you may ask for mathematical tables.
-

SECTION-A

1. Write 98 as product of its prime factors.
2. In fig. 1 the graph of a polynomial $p(x)$ is given. Find the zeroes of the polynomial.

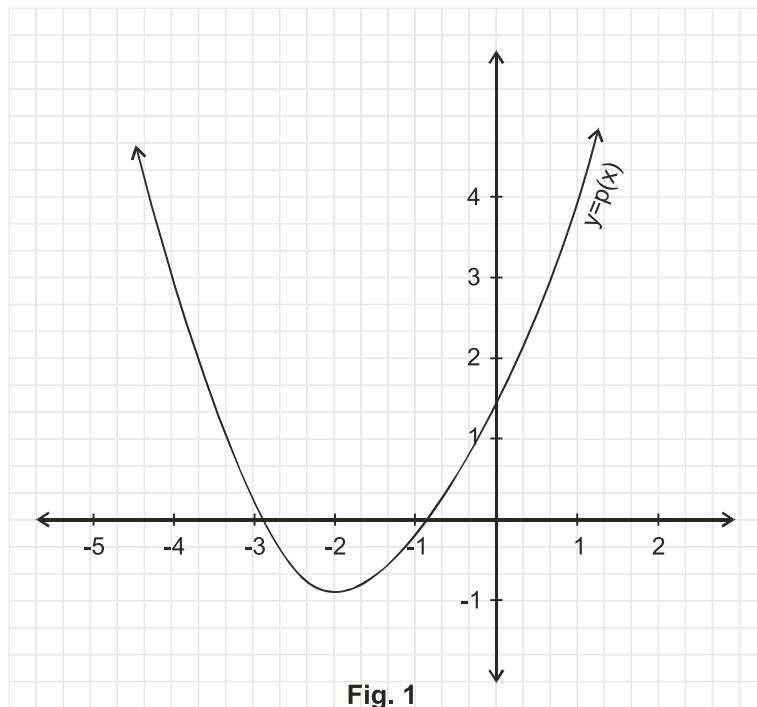


Fig. 1

3. For what value of k , the following pair of linear equations has infinitely many solutions?

$$10x + 5y - (k-5) = 0$$

$$20x + 10y - k = 0$$

4. What is the maximum value of $\frac{1}{\sec \theta}$?

5. If $\tan A = \frac{3}{4}$ and $A+B = 90^\circ$, then what is the value of $\cot B$?

6. What is the ratio of the areas of a circle and an equilateral triangle whose diameter and a side are respectively equal ?

7.

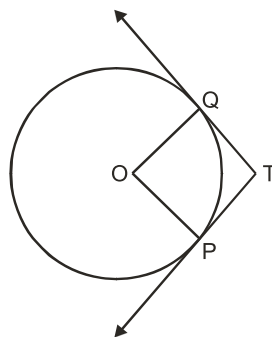


Fig. 2

Two tangents TP and TQ are drawn from an external point T to a circle with centre O, as shown in fig. 2. If they are inclined to each other at an angle of 100° then what is the value of $\angle POQ$?

8. In fig. 3 what are the angles of depression from the observing positions O_1 and O_2 of the object at A?

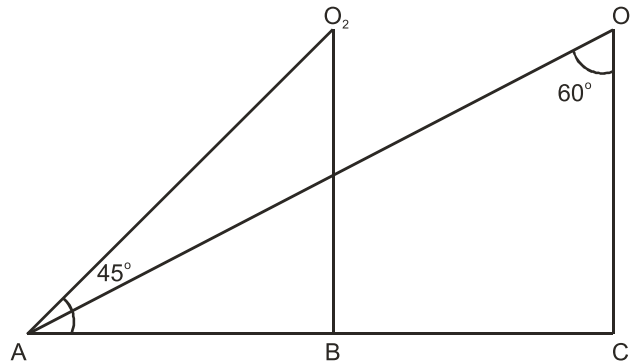


Fig. 3

9. A die is thrown once. what is the probability of getting a prime number?
10. What is the value of the median of the data using the graph in fig. 4, of less than ogive and more than ogive?

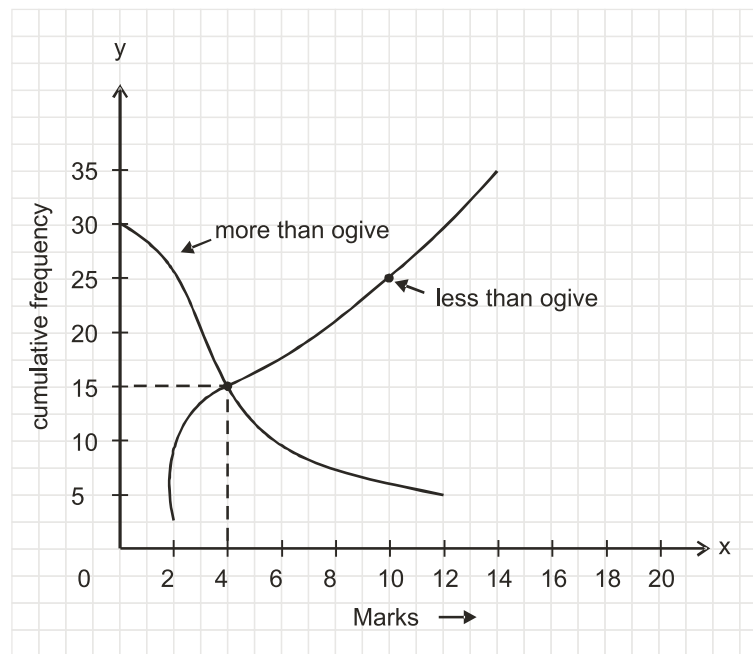


Fig. 4

SECTION : B

11. If the 10th term of an A.P. is 47 and its first term is 2, find the sum of its first 15 terms.
12. Justify the statement : "Tossing a coin is a fair way of deciding which team should get the batting first at the beginning of a cricket game."
13. Find the solution of the pair of equations:

$$\frac{3}{x} + \frac{8}{y} = -1, \quad \frac{1}{x} - \frac{2}{y} = 2, \quad x, y \neq 0$$

14. The coordinates of the vertices of $\triangle ABC$ are $A(4, 1)$, $B(-3, 2)$ and $C(0, k)$. Given that the area of ABC is 12 unit^2 , find the value of k .
15. Write a quadratic polynomial, sum of whose zeroes is $2\sqrt{3}$ and their product is 2.

OR

What are the quotient and the remainder, when $3x^4 + 5x^3 - 7x^2 + 2x + 2$ is divided by $x^2 + 3x + 1$?

SECTION-C

16. If a student had walked 1 km/hr faster, he would have taken 15 minutes less to walk 3 km. Find the rate at which he was walking.
17. Show that $3+5\sqrt{2}$ is an irrational number.
18. Find the value of k so that the following quadratic equation has equal roots:
 $2x^2 - (k-2)x + 1 = 0$
19. Construct a circle whose radius is equal to 4 cm. Let P be a point whose distance from its centre is 6 cm. Construct two tangents to it from P .
20. Prove that

$$\frac{\sin \theta}{\cot \theta + \operatorname{cosec} \theta} = 2 + \frac{\sin \theta}{\cot \theta - \operatorname{cosec} \theta}$$

OR

Evaluate

$$\frac{\sec 29^\circ}{\operatorname{cosec} 61^\circ} + 2 \cot 8^\circ \cot 17^\circ \cot 45^\circ \cot 73^\circ \cot 82^\circ - 3(\sin^2 38^\circ + \sin^2 52^\circ)$$

21. In fig. 5, $\frac{XP}{PY} = \frac{XQ}{QZ} = 3$, if the area of XYZ is 32 cm^2 , then find the area of the quadrilateral $PYZQ$.

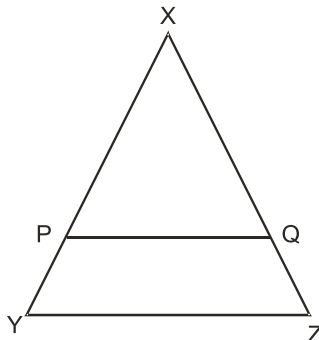


Fig. 5

OR

A circle touches the side BC of a $\triangle ABC$ at a point P and touches AB and AC when produced at Q and R respectively. Show that

$$AQ = \frac{1}{2} (\text{Perimeter of } \triangle ABC)$$

22. Find the ratio in which the line segment joining the points A (3, -6) and B(5,3) is divided by x - axis. Also find the coordinates of the point of intersection.
23. Find a relation between x and y such that the point P(x,y) is equidistant from the points A(2, 5) and B(-3, 7)
24. If in fig. 6, $\triangle ABC$ and $\triangle AMP$ are right angled at B and M respectively. prove that $CA \times MP = PA \times BC$

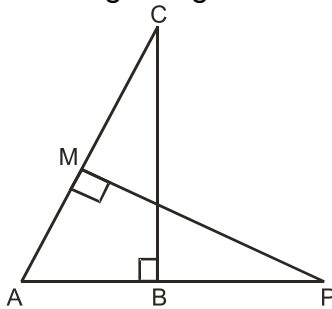


Fig. 6

25. In Fig. 7, OAPB is a sector of a circle of radius 3.5 cm with the centre at O and $\angle AOB = 120^\circ$. Find the length of OAPBO.

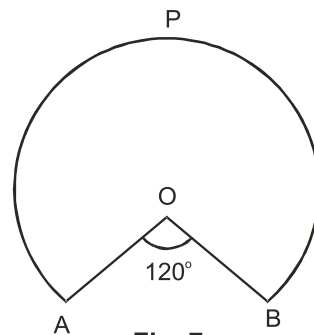


Fig. 7

OR

Find the area of the shaded region of fig. 8 if the diameter of the circle with centre O is

$$28 \text{ cm and } AQ = \frac{1}{4} AB.$$

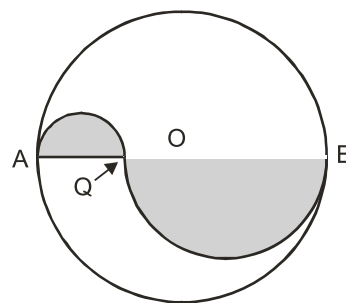


Fig. 8

SECTION-D

- [26] Prove that in a triangle, if the square of one side is equal to the sum of the squares of the other two sides the angle opposite to the first side is a right angle. Using the converse of above, determine the length of an altitude of an equilateral triangle of side 2 cm.
- [27] Form a pair of linear equations in two variables using the following information and solve it graphically.
Five years ago, Sagar was twice as old as Tiru. Ten year later Sagar's age will be ten years more than Tiru's age. Find their present ages. What was the age of Sagar when Tiru was born?
- [28] From the top and foot of a tower 40m high, the angle of elevation of the top of a light house is found to be 30° and 60° respectively. Find the height of the lighthouse. Also find the distance of the top of the lighthouse from the foot of the tower.
- [29] A solid is composed of a cylinder with hemispherical ends. If the whole length of the solid is 100cm and the diameter of the hemispherical ends is 28cm. find the cost of polishing the surface of the solid at the rate of 5 paise per sq.cm.

OR

An open container made up of a metal sheet is in the form of a frustum of a cone of height 8cm with radii of its lower and upper ends as 4 cm and 10 cm respectively. Find the cost of oil which can completely fill the container at the rate of Rs. 50 per litre. Also, find the cost of metal used, if it costs Rs. 5 per 100 cm^2 (Use $\pi = 3.14$)

- [30] The mean of the following frequency table is 53. But the frequencies f_1 and f_2 in the classes 20-40 and 60-80 are missing. Find the missing frequencies.

Age (in years)	0 - 20	20 - 40	40 - 60	60 - 80	80 - 100	Total
Number of people	15	f_1	21	f_2	17	100

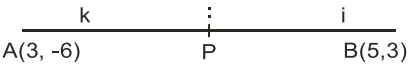
OR

Find the median of the following frequency distribution:

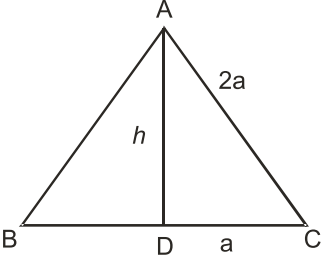
Marks	Frequency
0-100	2
100-200	5
200-300	9
300-400	12
400-500	17
500-600	20
600-700	15
700-800	9
800-900	7
900-1000	4

MARKING SCHEME III
X MATHEMATICS
SECTION A

Q.No	Value Points	Marks
1.	2×7^2	1
2.	- 3 and -1	1
3.	$k = 10$	1
4	one	1
5.	$\frac{3}{4}$	1
6.	$\pi : \sqrt{3}$	1
7.	$\angle POQ = 80^\circ$	1
8	$30^\circ, 45^\circ$	1
9.	$\frac{1}{2}$	1
10.	4	1
SECTION B		
11.	<p>Let a be first term and d be the common difference of the A.P.</p> <p>As we know that $a_n = a + (n - 1)d \Rightarrow 47 = 2 + 9d \Rightarrow d=5$</p> <p>$\therefore S_{15} = \frac{15}{2} [2 \times 2 + (15 - 1) 5] = 555$</p>	1 1
12.	<p>When we toss a coin, the outcomes head or tail are equally likely. So that the result of an individual coin toss is completely unpredictable. Hence both the teams get equal chance to bat first so the given statement is justified.</p>	1 1
13.	$\frac{3}{x} + \frac{8}{y} = -1,$(i)	

Q.No	Value Points	Marks
22.	<p>Let the ratio be $k : 1$ then the coordinates of the point which divides AB in the ratio $k : 1$ are</p> $\left(\frac{5k+3}{k+1}, \frac{3k-6}{k+1} \right)$  <p>This point lies on x - axis</p> $\frac{3k-6}{k+1} = 0$ $\Rightarrow k = 2$ <p>hence the ratio is 2:1</p> <p>Putting $k = 2$ we get the point of intersection</p> $\left(\frac{13}{3}, 0 \right)$	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>
23.	<p>Let P (x,y) be equidistant from the point A (2, 5) and B (-3, 7).</p> <p>$\therefore AP = BP$ so $AP^2 = BP^2$</p> $(x - 2)^2 + (y - 5)^2 = (x + 3)^2 + (y - 7)^2$ $x^2 - 4x + 4 + y^2 - 10y + 25 = x^2 + 6x + 9 + y^2 - 14y + 49$ $- 10x + 4y = 29$ <p>or $10x - 4y + 29 = 0$ is the required relation</p>	<p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>1</p> <p>1</p>
24.	<p>$\triangle AMP \sim \triangle ABC$</p> $\therefore \frac{PA}{CA} = \frac{MP}{BC}$ $\Rightarrow CA \times MP = PA \times BC$	<p>1</p> <p>$1\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>

Q.No	Value Points	Marks
25.	length of OAPBO = length of arc BPA + 2 (radius)	1
	$= \frac{240}{360} \times 2 \times \frac{22}{7} \times 3.5 + 2 \times 3.5$	1
	$= \frac{2}{3} \times 2 \times \frac{22}{7} \times \frac{7}{2} + 7$	
	$= 14 \frac{2}{3} + 7 = 21 \frac{2}{3}$	1
	Length of OAPBO = $21 \frac{2}{3}$ cm	
	OR	
	Diameter AQ = $\frac{1}{4} \times 28 = 7$ cm $\Rightarrow r_1 = \frac{7}{2}$ cm	$\frac{1}{2}$
	Diameter QB = $\frac{3}{4} \times 28 = 21$ cm $\Rightarrow r_2 = \frac{21}{2}$ cm	$\frac{1}{2}$
	area of shaded region = $= \frac{\pi}{2} \times \left[\left(\frac{7}{2} \right)^2 + \left(\frac{21}{2} \right)^2 \right]$	1
	$= \frac{\pi}{2} \times \left(\frac{7}{2} \right)^2 [1+3^2]$	
	$= \frac{1}{2} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} [10]$	
	$= \frac{77 \times 5}{2} = \frac{385}{2} = 192.5 \text{ cm}^2$	1

Q.No	Value Points	Marks
SECTION D		
26.	<p>Given, to prove, constand, figure</p> <p>Proof of theorem</p> <p>$AD \perp BC$</p> <p>$(2a)^2 = h^2 + a^2$</p> <p>$h^2 = 4a^2 - a^2$</p> <p>$h = \sqrt{3} a$</p> <p>$2a = 2 \Rightarrow a = 1 \text{ cm}$</p> <p>$\therefore h = \sqrt{3} \text{ cm}$</p>	<p>$\frac{1}{2} \times 4 =$</p> <p>2</p> <p>2</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p> <p>$\frac{1}{2}$</p>
		

27. Present age of sagar be x yrs & that of Tiru be y years.

$$x - 5 = 2(y - 5)$$

$$x - 2y + 5 = 0$$

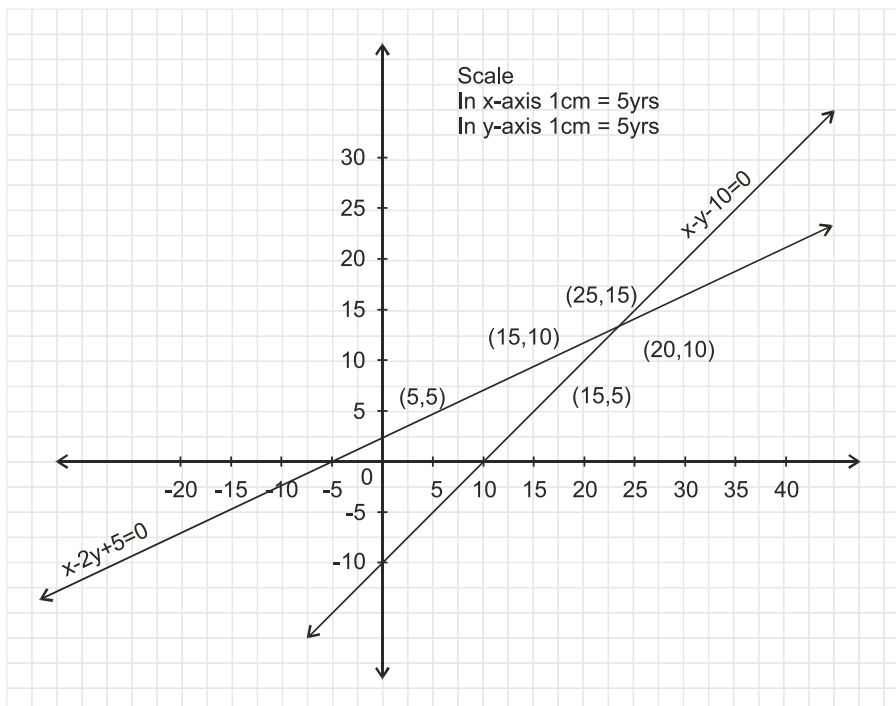
$$x + 10 = (y + 10) + 10$$

$$x - y - 10 = 0$$

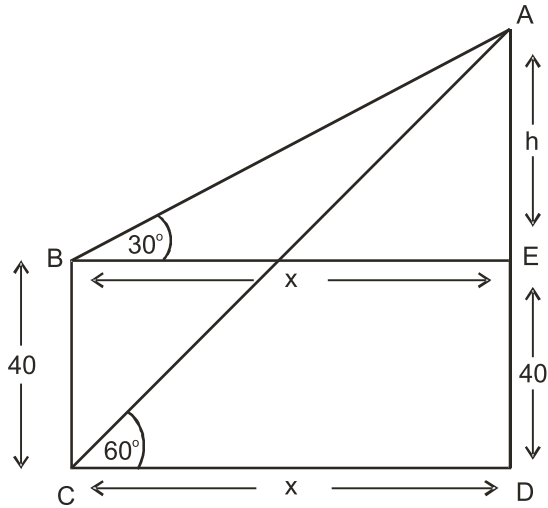
Equations : 1+1

x	5	15	25
y	5	10	15

x	15	20	25
y	5	10	15



Group : 1+1

Q.No	Value Points	Marks
28	<p>Since the lines intersect at (25, 15) Sagar's present age = 25 yrs, Tiru's present age = 15 yrs.</p>	<p>$\frac{1}{2}$ $\frac{1}{2}$</p>
	<p>From graph it is clear that Sagar was 10 years's old, when Tiru was born. 1</p>	<p>1</p>
		
	<p>For correct figure</p>	<p>1</p>
	<p>Let AE = h metre and BE = CD = x metre</p>	
	$\therefore \frac{x}{h} = \cot 30^\circ = \sqrt{3}$	<p>1</p>
	$\Rightarrow x = h\sqrt{3} \Rightarrow BE = CD = h\sqrt{3} \text{ m}$	<p>$\frac{1}{2}$</p>
	$\frac{h+40}{x} = \tan 60^\circ = \sqrt{3}$	
	$h+40 = \sqrt{3} \times h (\sqrt{3})$	<p>1</p>
	$h = 20\text{m}$	<p>$\frac{1}{2}$</p>
	<p>height of lighthouse is 20 + 40 = 60m</p>	<p>$\frac{1}{2}$</p>
	$\frac{AD}{AC} = \sin 60^\circ = \frac{\sqrt{3}}{2}$	<p>$\frac{1}{2}$</p>
	$\Rightarrow AC = 60 \frac{2}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$	<p>$\frac{1}{2}$</p>
	$\Rightarrow AC = 40\sqrt{3} \text{ m}$	
	<p>Hence the distance of the top of lighthouse from the foot of the tower is $40\sqrt{3} \text{ m}$</p>	<p>$\frac{1}{2}$</p>

Q .No	Value Points	Marks
29.	<p>Radius of hemisphere = 14cm.</p> <p>Length of cylindrical part = $[100 - 2(14)] = 72\text{cm}$</p> <p>radius of cylindrical part = radius of hemispherical ends = 14cm</p> <p>Total area to be polished</p> <p>= 2 (C.S.A. of hemispherical ends) + C.S.A. of cylinder</p> <p>= $2 (2 \pi r^2) + 2 \pi rh$</p> <p>= $2 \times \frac{22}{7} \times 14 (2 \times 14 + 72) = 8800\text{cm}^2$</p> <p>Cost of polishing the surface = Rs. 8800×0.05</p> <p>= Rs. 440</p> <p style="text-align: center;">OR</p> <p>The container is a frustum of a cone height 8cm and radius of the bases 10 cm and 4 cm respectively</p> <p>$h = 8\text{cm}, r_1 = 10\text{cm}, r_2 = 4\text{cm}$</p> <p>Slant height $l = \sqrt{8^2 + (10 - 4)^2} = \sqrt{8^2 + 6^2} = 10\text{cm}$</p> <p>Volume of container = $\frac{1}{3} \pi h (r_1^2 + r_2^2 + r_1 r_2)$</p> <p style="margin-left: 100px;">= $\frac{1}{3} \times 3.14 \times 8 (100 + 16 + 40) \text{cm}^3$</p> <p style="margin-left: 100px;">= $\frac{1}{3} \times 3.14 \times 8 (156)$</p> <p style="margin-left: 100px;">= $1306.24 \text{cm}^3 = 1.31 / \text{Litres (approx)}$</p> <p>Quantity of oil = 1.31/ Litres</p> <p>Cost of oil = Rs. (1.31×50)</p> <p style="margin-left: 40px;">= Rs. 65.50</p>	<p>1</p> <p>$\frac{1}{2}$</p> <p>1</p> <p>1</p> <p>1</p> <p>$\frac{1}{2}$</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p>

Q.No	Value Points	Marks																								
	<p>Surface area of the container (excluding the upper end)</p> $= \pi \times [l(r_1 + r_2) + r_2^2]$ $= 3.14 \times [10(10 + 4) + 16]$ $= 3.14 \times 156$ $= 489.84 \text{ cm}^2$ <p>cost of metal = Rs. $\left(489.84 \times \frac{5}{100}\right)$ =Rs 24.49</p>	<p>$\frac{1}{2}$</p> <p>1</p> <p>$\frac{1}{2}$</p>																								
30.	<table border="1" data-bbox="318 772 1284 1203"> <thead> <tr> <th>Age</th> <th>Number of people f_i</th> <th>Class mark(x_i)</th> <th>$x_i f_i$</th> </tr> </thead> <tbody> <tr> <td>0-20</td> <td>15</td> <td>10</td> <td>150</td> </tr> <tr> <td>20-40</td> <td>f_1</td> <td>30</td> <td>$30f_1$</td> </tr> <tr> <td>40-60</td> <td>21</td> <td>50</td> <td>1050</td> </tr> <tr> <td>60-80</td> <td>f_2</td> <td>70</td> <td>$70f_2$</td> </tr> <tr> <td>80-100</td> <td>17</td> <td>90</td> <td>1530</td> </tr> </tbody> </table> <p>$\sum f_i = 53 + f_1 + f_2 = 100$ $\sum x_i f_i = 2730 + 30 f_1 + 70 f_2$</p> <p>$\Rightarrow f_1 + f_2 = 47$ ----- (i)</p> $\bar{x} = \frac{\sum x_i f_i}{\sum f_i}$ $53 = \frac{2730 + 30 f_1 + 70 f_2}{100}$ <p>$\Rightarrow 3f_1 + 7f_2 = 257$ ----- (ii)</p> <p>Multiplying (i) by 3 and subtracting it from (ii) we get</p> $f_2 = 29$	Age	Number of people f_i	Class mark(x_i)	$x_i f_i$	0-20	15	10	150	20-40	f_1	30	$30f_1$	40-60	21	50	1050	60-80	f_2	70	$70f_2$	80-100	17	90	1530	<p>1</p> <p>1</p> <p>$\frac{1}{2}$</p> <p>1</p> <p>1</p>
Age	Number of people f_i	Class mark(x_i)	$x_i f_i$																							
0-20	15	10	150																							
20-40	f_1	30	$30f_1$																							
40-60	21	50	1050																							
60-80	f_2	70	$70f_2$																							
80-100	17	90	1530																							

Q .No	Value Points	Marks
	Put $f_2 = 29$ in (i) we get $f_1 = 18$ Hence $f_1 = 18$ and $f_2 = 29$	1 $\frac{1}{2}$
	OR	

Age	frequency	Cumulative frequency (C.F)
0 - 100	2	2
100 - 200	5	7
200 - 300	9	16
300 - 400	12	28
400 - 500	17	45
500 - 600	20	65
600 - 700	15	80
700 - 800	9	89
800 - 900	7	96
900 - 1000	4	100

$$N = \sum f_i = 100 \therefore \frac{N}{2} = 50$$

1

\therefore median class is 500 - 600

1

$$l = 500, f = 20, F = 45, h = 100$$

2

Hence

$$\text{Median} = l + \left(\frac{\frac{N}{2} - F}{f} \right) \times h$$

1

$$\text{Median} = 500 + \left(\frac{50 - 45}{20} \right) \times 100$$

$$\text{Median} = 525$$

1